

MATHEMATICS (H1)
Paper 1 Suggested Solutions

8864/01
October/November 2010

1. Topic: Equations & Inequalities (Quadratic Roots)

$$4x^2 - 2kx + 9 = 0$$

For two real distinct roots to exist, discriminant $b^2 - 4ac > 0$:

$$(-2k)^2 - 4(4)(9) > 0$$

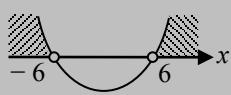
$$4k^2 - (12)^2 > 0$$

$$(2k-12)(2k+12) > 0$$

$$2k+12 < 0 \quad \text{or} \quad 2k-12 > 0$$

$$k < -6 \quad \text{or} \quad k > 6$$

For two real and *distinct* roots,
discriminant > 0 (no equal sign)
 $a = 4, b = -2k, c = 9$



\therefore The set of values of k for the equation to have two real and distinct roots is $\{k \in \mathbb{R} : k < -6 \text{ or } k > 6\}$

Note: Final answer expressed in set notation as question asks for set of values of k .

2. Topic: Integration

$$(i) \int e^{1-2x} dx = -\frac{1}{2}e^{1-2x} + c$$

$$\int e^{ax+b} dx = \frac{1}{a}e^{ax+b} + c$$

$$(ii) \int \frac{2}{(x+1)^3} dx = 2 \int (x+1)^{-3} dx$$

$$= (2) \frac{(x+1)^{-2}}{-2} + c$$

$$= -\frac{1}{(x+1)^2} + c$$

$$\int (ax+b)^n dx = \frac{(ax+b)^{n+1}}{a(n+1)} + c$$



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3. Topic: Graphs

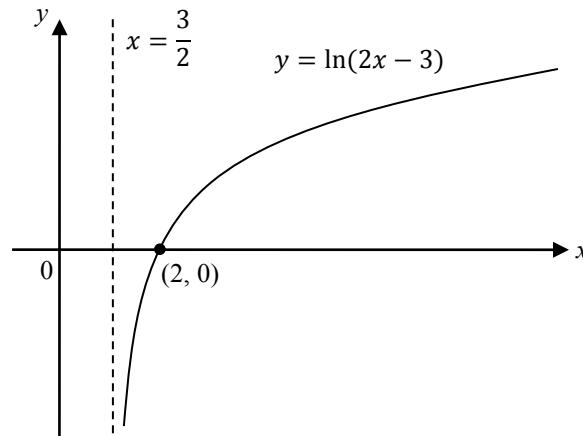
$$(i) y = \ln(2x-3) \Rightarrow \text{Equation of asymptote: } 2x-3 = 0 \Rightarrow x = \frac{3}{2}$$

Using G. C. (refer to Appendix for detailed steps),

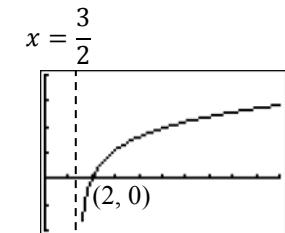
Plot1 Plot2 Plot3
Y1: $\ln(2x-3)$
Y2:
Y3:
Y4:
Y5:
Y6:
Y7:
SEL DEL TYPE STYL JMEM Draw

Graph Func.: Y= Y1: $\ln(2x-3)$ [—]
Y2:
Y3:
Y4:
Y5:
Y6:
Y7:
SEL DEL TYPE STYL JMEM Draw

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$$(ii) y = \ln(2x-3)$$

$$\frac{dy}{dx} = \frac{2}{2x-3}$$

$$\frac{d}{dx} \ln(ax+b) = \frac{a}{ax+b}$$



(iii) When $x = 3$,

$$y = \ln[2(3) - 3] = \ln 3$$

$$\text{Gradient of tangent, } m_T = \frac{2}{2(3)-3} = \frac{2}{3}$$

$$\Rightarrow \text{Gradient of normal, } m_N = -\frac{1}{m_T} = -\frac{3}{2}$$

Sub $x = 3$ into $\frac{dy}{dx}$ obtained in (ii).

∴ Equation of normal:

$$\begin{aligned} y - \ln 3 &= -\frac{3}{2}(x - 3) \\ 2y - 2\ln 3 &= -3x + 9 \\ 3x + 2y &= 9 + 2\ln 3 \end{aligned}$$

Equation of straight line with gradient m passing through (x_1, y_1) :
 $y - y_1 = m(x - x_1)$

4. Topic: Differentiation (Maxima & Minima)

(i) Given $AB = 2x$ m

$$\Rightarrow AE = \frac{5}{8}AB = \frac{5}{4}x \text{ m}$$

Since $ABCD$ is a rectangle,

$$\Rightarrow AD = BC$$

$$\Rightarrow DC = AB = 2x$$

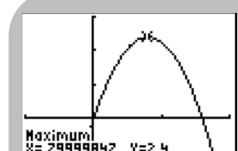
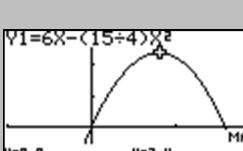
Given total perimeter $AEBCKA = 6$ m

$$AE + EB + BC + CD + AD = 6$$

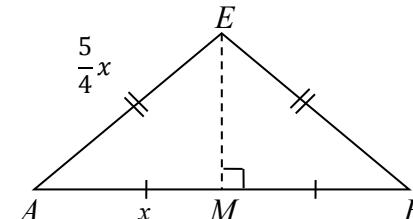
$$\frac{5}{4}x + \frac{5}{4}x + 2AD + 2x = 6$$

$$2AD = 6 - \frac{9}{2}x$$

$$AD = \left(3 - \frac{9}{4}x\right) \text{ m (shown)}$$

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Check final answer with G. C. (time permitting)

(ii) Since $\triangle AEB$ is isosceles,

$$AM = MB = x (EM \perp AB)$$

$$EM = \sqrt{\left(\frac{5}{4}x\right)^2 - x^2} = \frac{3}{4}x$$

By Pythagoras' theorem

∴ Area of the window, $A = \text{Area of } \triangle AEB + \text{Area of rectangle } ABCD$

$$\begin{aligned} &= \frac{1}{2}(2x)\left(\frac{3}{4}x\right) + (2x)\left(3 - \frac{9}{4}x\right) \\ &= \frac{3}{4}x^2 + 6x - \frac{9}{2}x^2 \\ &= \left(6x - \frac{15}{4}x^2\right) \text{ m}^2 (\text{shown}) \end{aligned}$$

Length of AD shown in part (i)

(iii) A is maximum when $\frac{dA}{dx} = 0$ i.e.

$$\frac{dA}{dx} = 6 - \frac{15}{2}x = 0$$

$$x = \frac{4}{5} \text{ m}$$

By 2nd derivative test, $\frac{d^2A}{dx^2} = -\frac{15}{2} < 0 \Rightarrow A$ is maximum when $x = \frac{4}{5}$.

$$\begin{aligned} \therefore A_{\max} &= 6\left(\frac{4}{5}\right) - \frac{15}{4}\left(\frac{4}{5}\right)^2 \\ &= \frac{12}{5} \text{ m}^2 \end{aligned}$$

Second Derivative Test:

Sign of $\frac{d^2y}{dx^2}$	Nature of stationary point
-	Maximum
+	Minimum
0	Point of inflection

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5. Topic : Applications of Differentiation & Integration

(i) Given $y = 6 - 4x^3 - 3x^4$

$$\frac{dy}{dx} = -12x^2 - 12x^3 = -12x^2(1+x)$$

At stationary points, $\frac{dy}{dx} = 0$

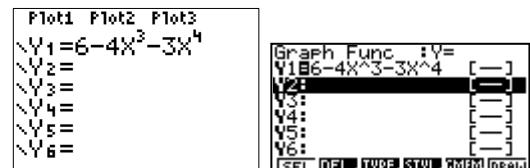
$$-12x^2(1+x) = 0$$

$$x = 0 \quad \text{or} \quad x = -1$$

$$y = 6 \quad \text{or} \quad y = 6 - 4(-1)^3 - 3(-1)^4 = 7$$

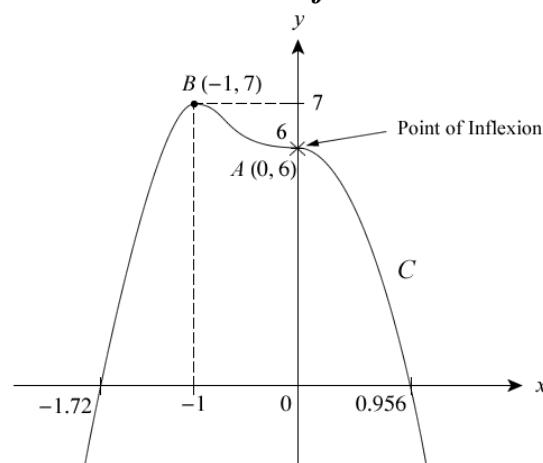
∴ Stationary points of curve C are **(0, 6)** and **(-1, 7)**

(ii) Using G. C. (refer to Appendix for detailed steps),



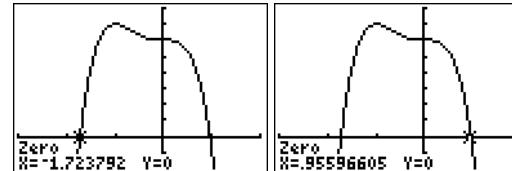
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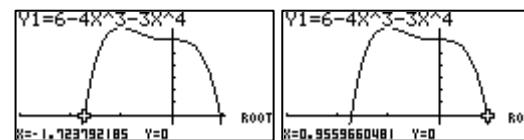


Final answer should be given in coordinates.

(iii) Using G. C. (refer to Appendix for detailed steps),



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∴ x-coordinates are **-1.72** (2d.p.) and **0.96** (2d.p.)

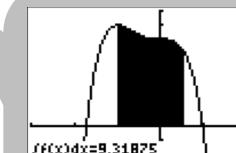
$$(iv) \int (6 - 4x^3 - 3x^4) dx = 6x - x^4 - \frac{3}{5}x^5 + c$$

$$\therefore \text{Area} = \int_{-1}^{\frac{1}{2}} (6 - 4x^3 - 3x^4) dx$$

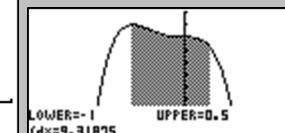
$$= \left[6x - x^4 - \frac{3}{5}x^5 \right]_{-1}^{\frac{1}{2}}$$

$$= \left[6\left(\frac{1}{2}\right) - \left(\frac{1}{2}\right)^4 - \frac{3}{5}\left(\frac{1}{2}\right)^5 \right] - \left[6(-1) - (-1)^4 - \frac{3}{5}(-1)^5 \right]$$

$$= 9\frac{51}{160} \text{ units}^2$$



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Check final answer with G. C. (time permitting)



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6. Topic: Probability (Venn Diagram)

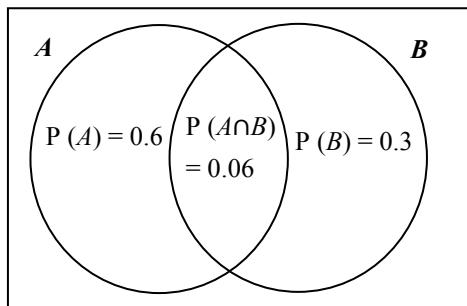
$$\begin{aligned} \text{(i)} \quad P(\text{both } A \text{ and } B \text{ occur}) &= P(A \cap B) \\ &= P(A|B)P(B) \\ &= 0.2 \times 0.3 \\ &= \mathbf{0.06} \end{aligned}$$

$$P(A|B) = \frac{P(A \cap B)}{P(B)}$$

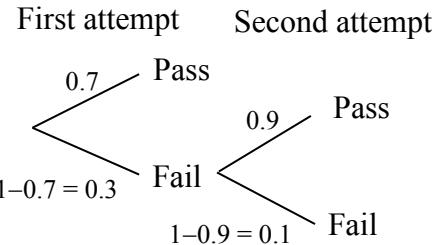
$$\begin{aligned} \text{(ii)} \quad P(\text{at least one of } A \text{ and } B \text{ occurs}) &= P(A \cup B) \\ &= P(A) + P(B) - P(A \cap B) \\ &= 0.6 + 0.3 - 0.06 \\ &= \mathbf{0.84} \end{aligned}$$

$$\begin{aligned} \text{(iii)} \quad P(\text{exactly one of } A \text{ and } B \text{ occurs}) &= P(A \cup B) - P(A \cap B) \\ &= 0.84 - 0.06 \\ &= \mathbf{0.78} \end{aligned}$$

Venn Diagram (for illustration):



7. Topic: Probability (Probability Tree)



$$\begin{aligned} \text{(i)} \quad P(\text{fails at both attempt}) &= 0.3 \times 0.1 \\ &= \mathbf{0.03} \end{aligned}$$

$$\text{(ii)} \quad P(\text{passes the examination}) = 1 - 0.03 = 0.97$$

$$\begin{aligned} P(\text{pass at 2nd attempt}) &= P(\text{fail on 1st attempt AND pass at 2nd attempt}) \\ &= 0.3 \times 0.9 = 0.27 \end{aligned}$$

P (pass at second attempt | passes the exam)

$$P(A|B) = \frac{P(A \cap B)}{P(B)}$$

$$\begin{aligned} &= \frac{P(\text{pass at 2nd attempt} \cap \text{passes the exam})}{P(\text{passes the exam})} \\ &= \frac{P(\text{pass at 2nd attempt})}{P(\text{passes the exam})} \\ &= \frac{0.27}{0.97} \\ &= \frac{27}{97} \end{aligned}$$

Pass at 2nd attempt
 \subseteq passes the exam

$$\begin{aligned} \text{(iii)} \quad P(\text{two pass at the 1st attempt and the other passes at 2nd attempt}) &= (0.7 \times 0.7) \times 0.27 \times 3 \text{ cases} \\ &= 0.3969 \\ &\approx \mathbf{0.397 \text{ (3 sig. fig.)}} \end{aligned}$$

3 Possibilities:
Case 1: 1st & 2nd students pass at 1st attempt
Case 2: 2nd & 3rd students pass at 1st attempt
Case 3: 3rd & 1st students pass at 1st attempt



**8. Topic: Sampling and Hypothesis Testing**

- (i) To obtain a stratified sample of 60 students, we divide the population into the following strata: Year One students, Year Two students and Year Three students.

We then pick random samples of the following sizes within each stratum:

$$\frac{1400}{3000} \times 60 = 28 \text{ Year One students}$$

$$\frac{900}{3000} \times 60 = 18 \text{ Year Two students}$$

$$\frac{700}{3000} \times 60 = 14 \text{ Year Three students}$$

Year One: $\frac{1400}{3000}$ of population

Year Two: $\frac{900}{3000}$ of population

Year Three: $\frac{700}{3000}$ of population

- (ii) Stratified sampling provides a more accurate representation of the large and varied student population, since the amount spent may vary according to year. As such, stratified sampling allows data for each year to be examined separately whereas this cannot be achieved with simple random sampling.

- (iii) Given $\Sigma x = 10450$, $\Sigma x^2 = 2235000$, $n = 50$.

$$\text{Unbiased estimate of } \mu = \frac{\Sigma x}{50} = \frac{10450}{50} = 209$$

Unbiased estimate of population mean,

$$\hat{\mu} = \frac{\Sigma x}{n}$$

$$\begin{aligned} \text{Unbiased estimate of } \sigma^2 &= \frac{1}{n-1} \left[\Sigma x^2 - \frac{(\Sigma x)^2}{n} \right] \\ &= \frac{1}{50-1} \left[2235000 - \frac{(10450)^2}{50} \right] \\ &= 1039\frac{39}{49} \end{aligned}$$

Unbiased variance estimate formula from MF15.

- (iv) 1. By the Central Limit Theorem, we assume that the amount of money spent by a student, X , is normally distributed, since the sample size is sufficiently large ($n \geq 50$).
2. Since σ^2 is not given, we assume that the value of the unbiased estimate of σ^2 computed in (iii) is sufficiently close to the actual population variance.

9. Topic: Binomial Distribution&ItsNormal Approximation

- (i) Let X be the random variable for the number of germinating sunflower seeds out of 8 sown, where

$$X \sim B(8, 0.7)$$

Binomial Distribution:

$X \sim B(n, p)$ where $n = \text{no. of trials} = 8$
 $p = \text{probability of success} = 0.7 \text{ (given)}$

Using G. C. (refer to Appendix for detailed steps),

TI-84 Plus
`binompdf(8,0.7,6
.29647548`

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`Binomial P.D.
Data :Variable
x :6
Numtrial:8
P :0.7
Save Res:None
Execute
[CALC]`

fx-9860G
`Binomial P.D.
P=0.29647548`

$$P(X = 6) = 0.29647 \approx 0.296 \text{ (3 sig.fig)}$$

- (ii) $P(X \geq 6) = 1 - P(X \leq 5)$

Using G. C. to calculate $P(X \leq 5)$ (refer to Appendix for detailed steps),

TI-84 Plus
`binomcdf(8,0.7,5
.4482261914`

fx-9860G
`Binomial C.D.
Data :Variable
x :5
Numtrial:8
P :0.7
Save Res:None
Execute
[CALC]`

fx-9860G
`Binomial C.D.
P=0.44822619`

$$\therefore P(X \geq 6) = 1 - 0.44823 = 0.55177 \approx 0.552 \text{ (3 sig.fig)}$$

G. C.'s binomial cumulative probability (CD) function is used.





Let Y be the random variable for the number of germinating sunflower seeds out of 60 sown, where $Y \sim B(60, 0.7)$.

Since $n = 60 > 50$ and $p = 0.7$,

$$np = 60 \times 0.7 = 42 > 5$$

$$nq = 60 \times (1 - 0.7) = 18 > 5$$

Since $np > 5$ and $nq > 5$, we use a normal distribution to approximate the binomial distribution with

$$E(Y) = np = 42$$

$$\text{Var}(Y) = npq = 60 \times 0.7 \times 0.3 = 12.6$$

$$\Rightarrow Y \sim N(42, 12.6) \text{ approximately}$$

$P(Y < 40) \rightarrow P(Y < 39.5)$ by continuity correction.

Using G. C. (refer to Appendix for detailed steps),

```
normalcdf(-e99, 39.5, 42, 12.6)
.2406243994
```

TI-84 Plus

```
Normal C.D
Lower: -1e+99
Upper: 39.5
σ: 3.54964786
μ: 42
Save Res:None
Execute
```

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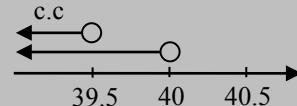
```
Normal C.D
P = 0.24062447
z:Low = -2.817e+98
z:Up = -0.7042952
```

When n is large and $np > 5$ and $nq > 5$,
 $X \sim N(n, p) \approx N(np, npq)$

$$\therefore P(Y < 40) = P(Y < 39.5) \text{ by Continuity Correction} \\ = 0.24062$$

 $\approx 0.241 \text{ (3 sig.fig)}$

Approximating a discrete distribution with a continuous distribution by Continuity Correction:



10. Topic: Hypothesis Testing

Let the random variable X be the mass of a components (in grams), and μ the mean mass, where $X \sim N(15, 1.2^2)$.

For a random sample of 80 components, $\bar{X} \sim N\left(15, \frac{1.2^2}{80}\right)$

To test $H_0: \mu = 15$ against

$H_1: \mu \neq 15$ at 5% of significance

Reject H_0 if $p\text{-value} < 0.05$.

Applying z-test with $\bar{x} = 15.25$, $n = 80$, $\sigma = 1.2$ using G. C. (refer to Appendix for detailed steps),

Z-Test
 Inpt: Data State
 $\mu_0: 15$
 $\sigma: 1.2$
 $\bar{x}: 15.25$
 $n: 80$
 $\mu: \text{Left} < \mu_0 > \mu_0$
 Calculate Draw

Z-Test
 $\mu \neq 15$
 $z = 1.863389981$
 $p = .062407292$
 $\bar{x} = 15.25$
 $n = 80$

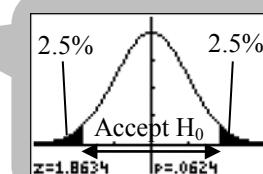
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I-Sample ZTest
 Data :Variable
 $\mu_0: \text{#}40$
 $\mu_0: 15$
 $\sigma: 1.2$
 $\bar{x}: 15.25$
 $n: 80$
 List Var

I-Sample ZTest
 $\mu = 15$
 $z = 1.86338998$
 $p = 0.06240741$
 $\bar{x} = 15.25$
 $n = 80$

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Testing for change in $\mu \Rightarrow$ Two-tailed test



From GC, the $p\text{-value} = 0.0624 > 0.05$, we do not reject H_0 .

Hence, there is insufficient evidence at the 5% significance level to conclude that the mean mass of the components is not 15 grams.



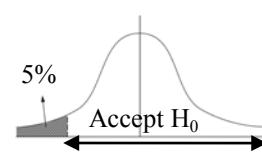
Under H_0 , $\bar{X} \sim N\left(15, \frac{1.2^2}{80}\right)$

To test $H_0 : \mu = 15$ against

$H_1 : \mu < 15$ at 5% of significance

Reject H_0 if z -value $< z_{0.05}$.

Testing for decrease in μ
i.e. $H_1: \mu < 15$, the critical region is in the lower tail of the distribution \Rightarrow left-tailed test



To obtain $z_{0.05}$, the critical value of z at 5%,

Using G. C. (refer to Appendix for detailed steps),

```
invNorm(.05, 0, 1)
-1.644853626
```

TI-84 Plus

$$z_{0.05} = -1.64485$$

```
Inverse Normal
Tail :Left
Area :0.05
σ :1
μ :0
Save Res:None
Execute
```

```
Inverse Normal
x=-1.6448536
```

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For H_0 to be rejected at 5% level of significance, test statistic

$$z = \frac{\bar{x} - \mu}{\frac{\sigma}{\sqrt{n}}} = \frac{\bar{x} - 15}{\frac{1.2}{\sqrt{80}}} < z_{0.05}$$

$$\frac{\bar{x} - 15}{\frac{1.2}{\sqrt{80}}} < -1.645$$

$$\bar{x} < 14.779$$

$$\bar{x} < 14.8 \text{ grams}$$

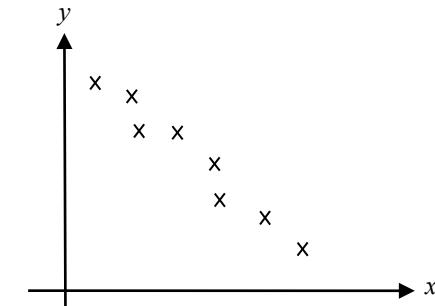
∴ Set of values: $\{\bar{x} \in \mathbb{R}^+ : \bar{x} < 14.78\}$

Note: Final answer expressed in set notation as question asks for set of values.

11. Topic: Correlation and Regression

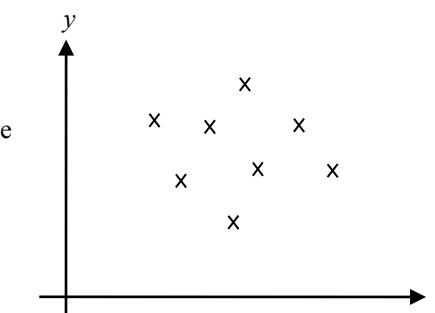
- (a) (i) Product moment correlation coefficient ≈ 0

\Rightarrow the eight points are randomly distributed with little or no pattern.



- (ii) Product moment correlation coefficient ≈ -0.8

\Rightarrow the eight points lie moderately close to a straight line with negative gradient.



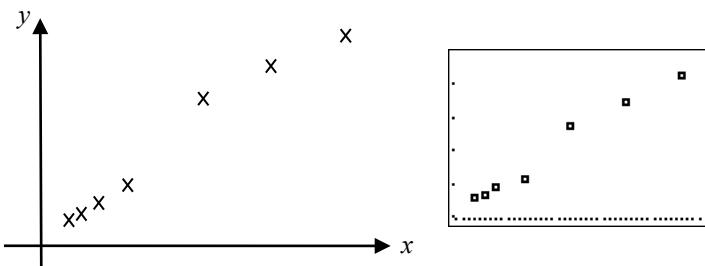
- (b) (i) Using G. C. (refer to Appendix for detailed steps),

L1	L2	L3	z
18	2.55		
20	2.65		
22	2.85		
23	3.15		
26	4.76		
46	5.45		
55	6.26		
L2(1)=2.55			

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SUB	List 1	List 2	List 3	List 4
1	18	2.55		
2	20	2.65		
3	22	2.85		
4	23	3.15		

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- (ii) Using G. C. (refer to Appendix for detailed steps),

```
LinReg
y=ax+b
a=.1069341463
b=.5615170732
r^2=.9747520719
r=.9872953317
```

TI-84 Plus

$$r = 0.98729 \approx 0.987 \text{ (3 sig.fig)}$$

```
LinearReg
a =0.10693414
b =0.56151707
r =0.98729533
r^2=0.97475207
MSe=0.06939207
y=ax+b
```

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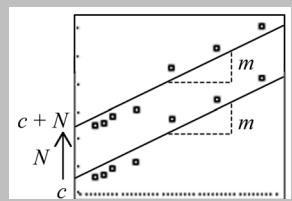
- (iii) Sub values of a and b obtained by G.C. in part (ii) into m and c respectively $\Rightarrow y = 0.1069x + 0.5615$

- (iv) When $x = 40$, $y = 0.1069(40) + 0.5615 = 4.8375 \approx 4.84$ (3 sig. fig.)
 \therefore Estimated monthly earnings of a 40-year-old worker is \$4840.

Note: y is in thousand dollars!

Since $x = 40$ is within the range of given data values [18, 55], the estimate is reliable as we are interpolating within the data range.

- (v) m will remain the same and the constant c becomes $(c + N)$.



Remember to square the standard deviations when calculating the variance!

12. Topic: Normal Distribution

- (i) Let U be the random variable for the mass of an unwrapped sweet, where $U \sim N(40, 3^2)$

Using G. C. (refer to Appendix for steps to access the normal distribution functions),

```
normalcdf(-E99, 3
6, 40, 3)
.0912112819
```

```
Normal C.D
Lower : -1E+99
Upper : 36
σ : 3
μ : 40
Save Res:None
Execute |CALC|
```

```
Normal C.D
P = 0.09121121
z:Low=-3.33E+98
z:Up = -1.333333333
```

TI-84 Plus**fx-9860G**

$$P(U < 36) = 0.091211 \approx 0.0912 \text{ (3 sig.fig)}$$

- (ii) Let W be the random variable for the mass of a wrapper, where $W \sim N(4, 0.5^2)$

Let S be the random variable for the mass of a wrapped sweet.

$$E(S) = E(U) + E(W) = 40 + 4 = 44$$

$$\text{Var}(S) = \text{Var}(U) + \text{Var}(W) = 3^2 + 0.5^2 = 9.25$$

$$\therefore S \sim N(44, 9.25)$$

Using G. C. (refer to Appendix for steps to access the normal distribution functions),

```
normalcdf(42, 46,
44, √(9.25))
.4892023398
```

```
Normal C.D
Lower : 42
Upper : 46
σ : 3.04138126
μ : 44
Save Res:None
Execute |CALC|
```

```
Normal C.D
P = 0.48920222
z:Low=-0.6575959
z:Up = 0.65759594
```

TI-84 Plus**fx-9860G**

$$P(42 < S < 46) = 0.48920 \approx 0.489 \text{ (3 sig.fig)}$$





- (iii) Let C be the random variable for the mass of an empty cardboard tube, where $C \sim N(50, 5^2)$.

Let T be the random variable for the total mass of a tube containing 12 wrapped sweets.

$$\begin{aligned} T &= S_1 + S_2 + \dots + S_{12} + C \\ E(T) &= E(S_1 + S_2 + \dots + S_{12}) + E(C) \\ &= 12E(S) + E(C) \\ &= 12 \times 44 + 50 = 578 \\ \text{Var}(T) &= \text{Var}(S_1 + S_2 + \dots + S_{12}) + \text{Var}(C) \\ &= 12\text{Var}(S) + \text{Var}(C) \\ &= 12 \times 9.25 + 5^2 = 136 \\ T &\sim N(578, 136) \end{aligned}$$

Using G. C. (refer to Appendix for steps to access the normal distribution functions),

```
normalcdf(600, e9
9,578, f(136))
.0296147861
```

TI-84 Plus

```
Normal C.D
Lower :600
Upper :1e+99
σ :11.6619037
μ :578
Save Res:None
Execute
None LIST
```

fx-9860G

$$\therefore P(T > 600) = 0.029614 \approx 0.0296 \text{ (3 sig.fig)}$$

- (iv) Let Y be the random variable for the total mass of a tube containing 12 wrapped sweets produced by the rival company, where $Y \sim N(\mu, \sigma^2)$.

$$\text{Given } P(Y < 450) = 0.05 \quad \text{and} \quad P(Y > 550) = 0.08$$

$$P\left(Z < \frac{450-\mu}{\sigma}\right) = 0.05 \quad P\left(Z > \frac{550-\mu}{\sigma}\right) = 0.08$$

If $X_1, X_2, X_3, \dots, X_n$ are n independent observations of the normal variable X where $X \sim N(\mu, \sigma^2)$,

$$X_1 + X_2 + X_3 + \dots + X_n \sim N(n\mu, n\sigma^2)$$

N.B. n is NOT squared for the variance! This is different from $nX \sim N(n\mu, n^2\sigma^2)$!

Using G. C. (refer to Appendix for detailed steps),

```
invNorm(0.05)
-1.644853626
```

TI-84 Plus

```
invNorm(0.92)
1.405071561
```

TI-84 Plus

```
Inverse Normal
Tail :Left
Area :0.05
σ :1
μ :0
Save Res:None
Execute
CALC
```

fx-9860G

```
Inverse Normal
x=-1.6448536
```

```
Inverse Normal
Tail :Right
Area :0.92
σ :1
μ :0
Save Res:None
Execute
CALC
```

fx-9860G

$$\frac{450-\mu}{\sigma} = -1.64485 \quad \frac{550-\mu}{\sigma} = 1.40507$$

$$\mu = 450 + 1.64485\sigma \dots (1) \quad 550 - \mu = 1.40507\sigma \dots (2)$$

$$\text{Sub (1) into (2): } 550 - 450 - 1.64485\sigma = 1.405076$$

$$\sigma = 32.7877 \Rightarrow \sigma^2 = 1075.0 \approx 1080$$

$$\Rightarrow \mu = 503.9309 \approx 504$$

∴ Mean ≈ 504 and variance ≈ 1080 (3 sig.fig)



Appendix: Detailed G. C. Steps (for those still trapped in G. C. limbo)

Q3 (i), 5 (ii): Graph Sketching

TI-84 Plus

MODE

→ Ensure G. C. is in **FUNC** mode.

```

NORMAL SCI ENG
FLOAT 0 1 2 3 4 5 6 7 8 9
RADIAN DEGREE
FUNC PAR POL SEQ
CONNECTED DOT
SEQUENTIAL SIMUL
REAL a+bi re^θi
FULL HORIZ G-T
SETCLOCK 08/16/11 7:50PM

```

Y= **WINDOW** **GRAPH**

```

Plot1 Plot2 Plot3
Y1: ln(2X-3)
Y2:
Y3:
Y4:
Y5:
Y6:
Y7:

```

```

Plot1 Plot2 Plot3
Y1: 6-4X^3-3X^4
Y2:
Y3:
Y4:
Y5:
Y6:

```

```

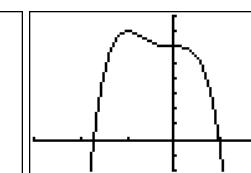
WINDOW
Xmin=0
Xmax=10
Xscl=1
Ymin=-2
Ymax=4
Yscl=1
Xres=1

```

```

WINDOW
Xmin=-3
Xmax=2
Xscl=1
Ymin=-2
Ymax=8
Yscl=1
Xres=1

```

**fx-9860G**

```

MAIN MENU
GRAPH DYNAMIC TABLE RECUR
CONICS EQUA PRGM TVM

```

```

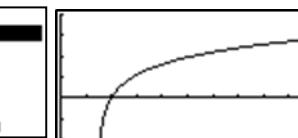
Graph Func :Y=
Y1:ln (2X-3) [—]
Y2:
Y3:
Y4:
Y5:
Y6:
SEL DEL TYPE STYL MEM DRAW

```

```

View Window
Xmin :0
max :10
scale:1
dot :0.07936507
Ymin :-2
max :4
INIT TRIG STD STO RCL

```



[SHIFT] ↑

[EXIT] [F6]

```

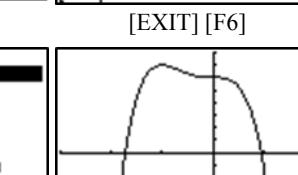
Graph Func :Y=
Y1:6-4X^3-3X^4 [—]
Y2:
Y3:
Y4:
Y5:
Y6:
SEL DEL TYPE STYL MEM DRAW

```

```

View Window
Xmin : -3
max :2
scale:1
dot :0.03968253
Ymin :-2
max :8
INIT TRIG STD STO RCL

```



[SHIFT] ↑

[EXIT] [F6]

Q5 (iii): Finding the Roots of a Function

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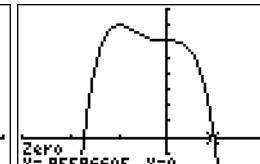
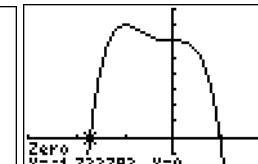
**TI-84 Plus Method I: Using Zero Values of Graphs**

Y=
2nd **TRACE** **2**

- Define approximate left/right bounds of value for 1st root.
- Repeat steps for 2nd root.

Plot1 Plot2 Plot3
 $\text{Y}_1 = 6 - 4X^3 - 3X^4$
 $\text{Y}_2 =$
 $\text{Y}_3 =$
 $\text{Y}_4 =$
 $\text{Y}_5 =$
 $\text{Y}_6 =$

CALCULATE
1:value
2:zero
3:minimum
4:maximum
5:intersect
6:dy/dx
7:fn(x)dx



Note: This is the preferred method for Q5(iii) since we are already in Graphing mode having just sketched C in part (ii).

Method II: Using Solver

MATH

- Enter **Solver** (last item on MATH menu)
- Enter equation.
- Enter an approximate value of x (i.e. $x = -1.5$) for 1st root.
- Enter an approximate value of x (i.e. $x = 1$) for 2nd root.

ALPHA **ENTER**

MATH NUM CPX PRB
6:fMin()
7:fMax()
8:nDeriv()
9:fnInt()
0:summation Σ<
A:logBASE()
B:Solver...

EQUATION SOLVER
 $\text{eqn}: 0 = 6 - 4X^3 - 3X^4$
4

$6 - 4X^3 - 3X^4 = 0$
 $X = -1.5$ bound=(-1e99, 1...)

$6 - 4X^3 - 3X^4 = 0$
 $X = -1.723792185$ bound=(-1e99, 1...)
left-rt=0

$6 - 4X^3 - 3X^4 = 0$
 $X = 1$ bound=(-1e99, 1...)
left-rt=0

$6 - 4X^3 - 3X^4 = 0$
 $X = .95596604812$ bound=(-1e99, 1...)
left-rt=0

Method III: Using Poly Root Finder Application

APPS

- Enter **PlySmlt2**

APPLICATIONS
1:Finance...
2:Conics
3:CtlgHelp
4:Inequalz
5:PlySmlt2
6:Transfrm

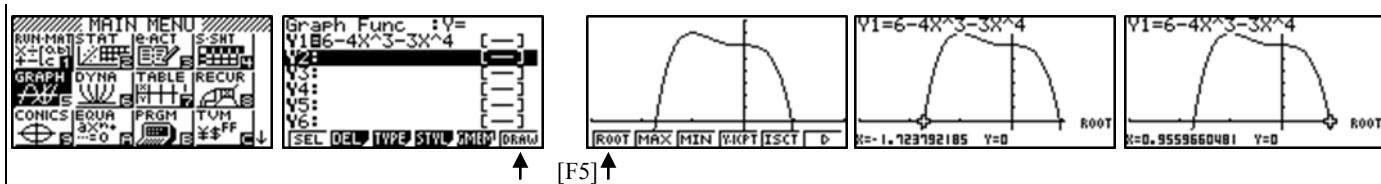
MAIN MENU
1: POLY ROOT FINDER
2: SIMULT EQN SOLVER
3: ABOUT
4: POLY HELP
5: SIMULT HELP
6: QUIT POLYSMLT
MATRIX (HELP/NEXT)

POLY ROOT FINDER MODE
ORDER 1 2 3 4 5 6 7 8 9 10
REAL a+bi re^(θi)
DEC FRAC
NORMAL SCI ENG
FLOAT 0 1 2 3 4 5 6 7 8 9
RADIANT DEGREE
MATRIX (HELP/NEXT)

$a_4x^4 + a_3x^3 + a_2x^2 + a_1x + a_0 = 0$
 $a_4 = -3$
 $a_3 = -4$
 $a_2 = 0$
 $a_1 = 0$
 $a_0 = 6$
MATRIX (HELP/NEXT)

$a_4x^4 + a_3x^3 + a_2x^2 + a_1x + a_0 = 0$
 $x_1 = -1.723792185$
 $x_2 = -.282753598$
 $x_3 = -.282753598$
 $x_4 = .9559660481$
MATRIX (HELP/NEXT)

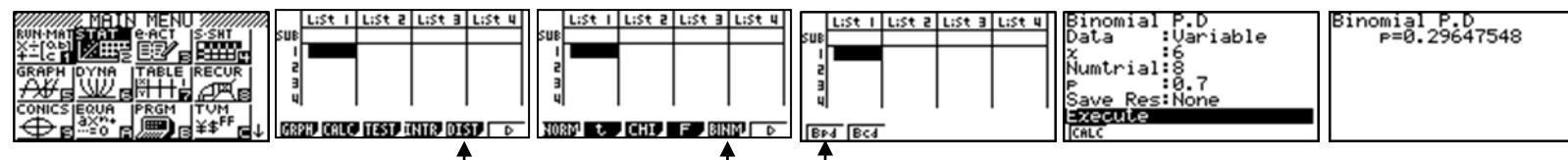


**fx-9860G Find Roots in Graph****Q9 (i): Binomial Distribution (Computing Probability)****TI-84 Plus**
2nd VARS ALPHA MATH

→ Key in the parameters.

```
0:DISP DRAW
6:tcdcf(
7:X2Pdf(
8:X2Cdf(
9:Fpdf(
0:Fcdf(
A:binompdf(
B:binomcdf(
```

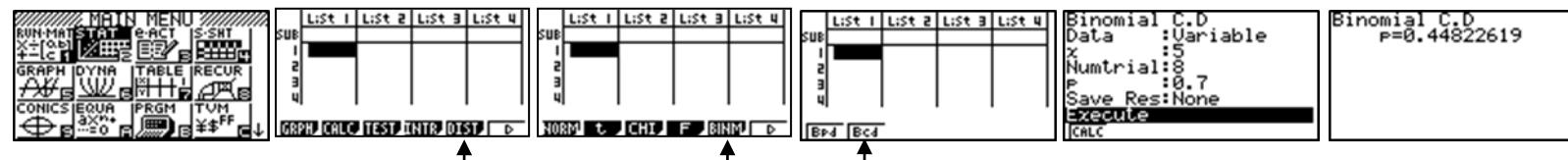
binompdf(8,0.7,6
.29647548

fx-9860G**Q9 (ii): Binomial Distribution (Computing Cumulative Probability)****TI-84 Plus**
2nd VARS ALPHA APPS

→ Key in the parameters.

```
0:DISP DRAW
6:tcdcf(
7:X2Pdf(
8:X2Cdf(
9:Fpdf(
0:Fcdf(
A:binompdf(
B:binomcdf(
```

binomcdf(8,0.7,5
.4482261914

fx-9860G

**Q9, Q12(i), (ii), (iii): Normal Distribution****TI-84 Plus**

2nd

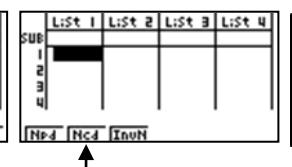
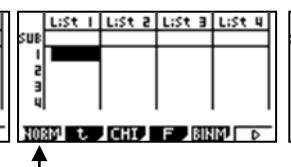
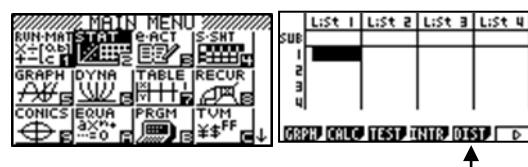
VARS

2

→ Key in the relevant parameters. Results shown are for Q9

```
DISTR DRAW
1:normalPdf(
2:normalCdf(
3:invNorm(
4:invT(
5:tPdf(
6:tCdf(
7:tX2Pdf(
```

```
normalCdf(-e99, 39.5, 42, √(12.6))
.2406243994
```

fx-9860G

```
Normal C.D
Lower : -1e+99
Upper : 39.5
σ : 3.54964786
μ : 42
Save Res:None
Execute
```

```
Normal C.D
P = 0.24062447
z:Low = -2.817e+98
z:Up = -0.7042952
```

Q10, Q12 (iv): Finding z-value**TI-84 Plus**

2nd

VARS

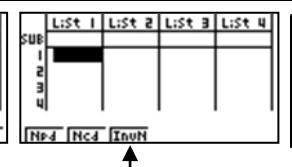
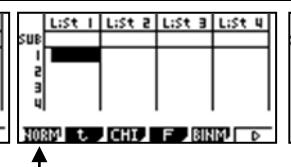
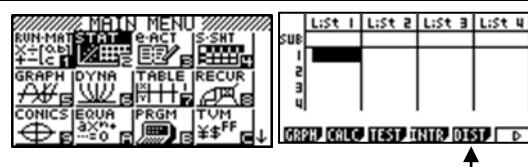
3

→ Key in the desired probability /level of significance. Results shown are for Q10

```
DISTR DRAW
1:normalPdf(
2:normalCdf(
3:invNorm(
4:invT(
5:tPdf(
6:tCdf(
7:tX2Pdf(
```

```
invNorm
area: 0.05
μ: 0
σ: 1
Paste
```

```
invNorm(.05, 0, 1)
-1.644853626
```

fx-9860G

```
Inverse Normal
Tail : Left
Area : 0.05
σ : 1
μ : 0
Save Res:None
Execute
```

```
Inverse Normal
x = -1.6448536
```



Q10: Hypothesis Testing (z-Test with Data Summary)**TI-84 Plus**

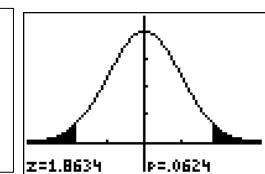
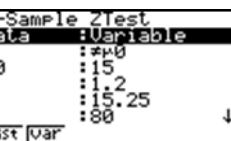
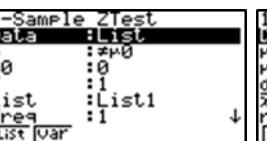
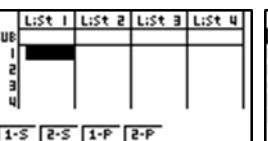
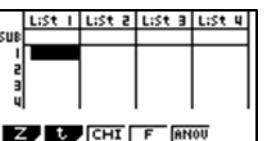
- Select **Stats** input method.
- Enter the population/sample mean, σ (variance), sample size.
- Select $\mu \neq \mu_0$ for two-tailed test.

ENTER

- Select **Calculate** for results in summary view.
- Select **Draw** for results in graphical view.

EDIT CALC TEST
 1:Z-Test...
 2:T-Test...
 3:2-SampZTest...
 4:2-SampTTest...
 5:1-PropZTest...
 6:2-PropZTest...
 7:ZInterval...

Z-Test
 Inpt:Data Stats
 $\mu_0: 15$
 $\sigma: 1.2$
 $\bar{x}: 15.25$
 $n: 80$
 $\mu: \neq \mu_0 < \mu_0 > \mu_0$
 Calculate Draw

Z-Test
 $\mu \neq 15$
 $z=1.863389981$
 $p=.062407292$
 $\bar{x}=15.25$
 $n=80$
**fx-9860G**

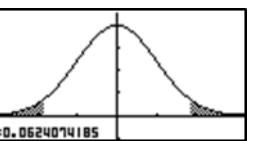
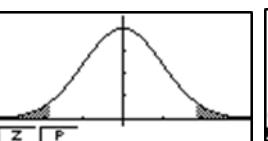
[Enter the parameters]

1-Sample ZTest
 $\mu_0: 15$
 $\sigma: 1.2$
 $\bar{x}: 15.25$
 $n: 80$
 Save Res:None
 Execute

1-Sample ZTest
 $\mu: \neq 15$
 $z: 1.86338998$
 $p: 0.06240741$
 $\bar{x}: 15.25$
 $n: 80$
 Save Res:None
 Execute

1-Sample ZTest
 $\mu_0: 15$
 $\sigma: 1.2$
 $\bar{x}: 15.25$
 $n: 80$
 Save Res:None
 Execute

Results (summary view)



Results (graphical view)


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Q11 (b)(i): Plotting Scatter Diagram**TI-84 Plus****STAT** **ENTER**

→ Enter xandy values in L1 and L2 respectively

CALC TESTS

L1	L2	L3	Z
18	2.55	-----	
20	2.65		
22	2.85		
27	3.15		
35	4.75		
45	5.45		
55	6.25		

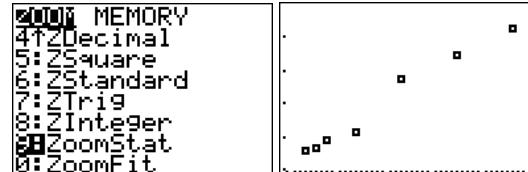
L2(1)=2.55

2nd **Y=** **ENTER**

→ Turn On Plot1

STAT PLOTS

1:Plot1...Off	2:Plot2...Off	3:Plot3...Off
4:PlotsOff	Type: Scatter	Xlist: L1
	Ylist: L2	Mark: +

ZOOM **9****fx-9860G**

MAIN MENU

GRAPH	DYNA	TABLE	RECUR
CONICS	EQUA	PRGM	TVM
S	3XN+	B	Y=\$FF

LIST 1	LIST 2	LIST 3	LIST 4
1 18	2.55		
2 20	2.65		
3 22	2.85		
4 27	3.15		

GRPH **CALC** **TEST** **INTR** **DIST**

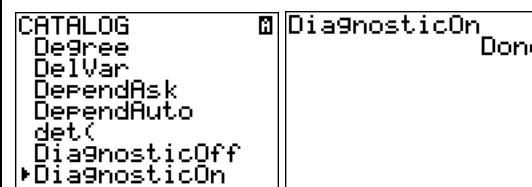
LIST 1	LIST 2	LIST 3	LIST 4
1 18	2.55		
2 20	2.65		
3 22	2.85		
4 27	3.15		

GRPH1 **GRPH2** **GRPH3** **SEL** **SET**

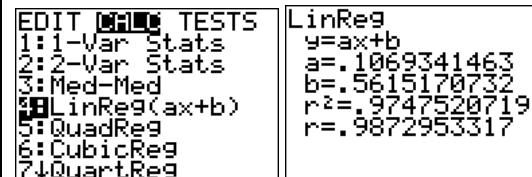


**Q11 (b)(ii): Finding Correlation Coefficient****TI-84 Plus**

Note: The r value will not appear if you miss this step!



Note: L1 contains the values of x (independent variable) and L2 the values of y (dependent variable) as populated in 11(b)(i).

**fx-9860G**